

**While loop, Decimal 2 Binary**  
**Fabonacci series**  
**Prime factor**

# **While looping Decimal to Binary**

While迴圈的進入條件要如何設計呢？

```
import random
N = 100000
S = list(range(1,N))
n = random.choice(S)
print(bin(n))
print("converting",n," to")
b = ""
while n > 0:
    r = n % 2
    b = str(r) + b
    n = (n - r) // 2
print("0b"+b)
```

While迴圈中的主體命令要如何設計呢？

While迴圈和for迴圈有什麼不一樣呢？

為什麼需要使用while迴圈？難道不能只使用for迴圈，就好了呢？

```
0b10100100001000110
converting 84038 to
0b10100100001000110
```

10.7

```
while n > 0:  
    r = n % 2  
    b = str(r) + b  
    n = (n - r) // 2
```

迴圈	進入條件 n>0	r	n	b
初始值			11	""
迴圈1	T	1	5	"1"
迴圈2	T	1	2	"11"
迴圈3	T	0	1	"011"
迴圈4	T	1	0	"1011"
迴圈5	<b>F</b>			

```

b = ""
n = 11
while n > 0:
    r = n % 2
    b = str(r) + b
    n = (n - r) // 2
    print(n>0, " r:",r," n:",n," b:",b)
print("0b"+b)

```

```

True r: 1 n: 5 b: 1
True r: 1 n: 2 b: 11
True r: 0 n: 1 b: 011
False r: 1 n: 0 b: 1011
0b1011

```

迴圈	進入條件 n>0	r	n	b
初始值			11	""
迴圈1	T	1	5	"1"
迴圈2	T	1	2	"11"
迴圈3	T	0	1	"011"
迴圈4	T	1	0	"1011"
迴圈5	F			

```

b = ""
n = 23
while n > 0:
    r = n % 2
    b = str(r) + b
    n = (n - r) // 2
    print(n>0, " r:",r, " n:",n, " b:",b)
print("0b"+b)

```

```

True  r: 1  n: 11  b: 1
True  r: 1  n: 5   b: 11
True  r: 1  n: 2   b: 111
True  r: 0  n: 1   b: 0111
False r: 1  n: 0   b: 10111
0b10111

```

迴圈	進入條件 n>0	r	n	b
初始值			23	""
迴圈1	T	1	11	"1"
迴圈2	T	1	5	"11"
迴圈3	T	1	2	"111"
迴圈4	T	0	1	"0111"
迴圈5	T	1	0	"10111"
迴圈6	F			

# 列印小於 $n$ 的Fabonacci 數列

# Fabonacci數列

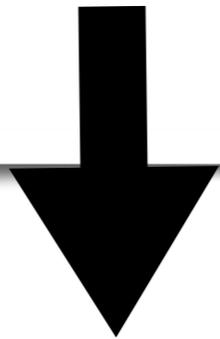
26  
0 1 1 2 3 5 8 13 21

The diagram illustrates the recursive property of the Fibonacci sequence. It shows the sequence 0, 1, 1, 2, 3, 5, 8, 13, 21. Below the sequence, three red boxes are arranged in a row:  $a_4$ ,  $a_5$ , and  $a_6$ . The boxes for  $a_4$  and  $a_5$  are connected by a plus sign (+), and the box for  $a_6$  is connected by an equals sign (=). Red arrows point from the top of the  $a_4$  and  $a_5$  boxes to the number 3 in the sequence, and from the top of the  $a_6$  box to the number 5 in the sequence.

$$a_4 + a_5 = a_6$$

# Fabonacci數列

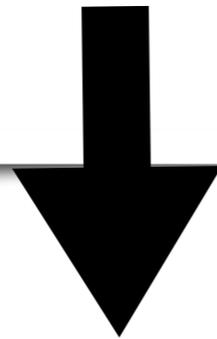
26  
0 1 1 2 3 5 8 13 21



n	a	b
4	3	5

# Fabonacci數列

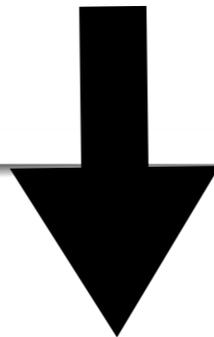
26  
0 1 1 2 3 5 8 13 21



n	a	b
4	3	5
5	5	8

# Fabonacci數列

26  
0 1 1 2 3 5 8 13 21



n	a	b
4	3	5
5	5	8
6	8	13

如何在迴圈中更新a與b？

設定a, b的初始值

**while**

進入條件

```
print(a, end = '')  
使用現有的a與b值  
更新a與b值
```

```
import random
Dice = list(range(1,53))
n = random.choice(Dice)
print(n)
```

```
a, b = 0, 1
```

```
while a < n:
```

```
print(a, end = ' ')
a, b = b, a+b
```

設定a, b的初始值

**while**

進入條件

```
print(a, end = ' ')
使用現有的a與b值
更新a與b值
```

# Fabonacci數列

26  
0 1 1 2 3 5 8 13 21

```
while a < n:
```

```
print(a, end = ' ')  
a, b = b, a+b
```

n	a	b
4	3	5
5	5	8
6	8	13
7	13	21

如何在迴圈中更新a與b？

```
import random
Dice = list(range(1,53))
n = random.choice(Dice)
print(n)
a, b = 0, 1
while a < n:
    print(a, end = ' ')
    a, b = b, a+b
print()
```

23

0 1 1 2 3 5 8 13 21

**產生小於n的Fabonacci  
數列，並儲存在串列中**

```
n = 35  
result = []  
a, b = 0, 1
```

An empty  
array

```
while a < n:  
    result.append(a)  
    a, b = b, a+b  
print(result)
```

Add a Fab number to  
array result

```
[0, 1, 1, | 2, 3, 5, 8, 13, 21]
```

找n的所有質因數

找n的最小質因數

```
import random
S = list(range(1,100000))
n = random.choice(S)
for a in range(2,n):
    if n % a == 0:
        m = n//a
        print(n, 'equals', a, '*', m)
        break
    else:
        print(n, 'is a prime number')
        a = n
        m = 1
```

```
import random
import numpy as np
S = list(range(1,100000))
n = random.choice(S)
for x in range(2,int(np.ceil(n/2))):
    if n % x == 0:
        print('n = ', n, ' a = ', x)
        break
else:
    print(n, ' is a prime')
```

## 步驟

1. 輸入 $n$ ，設定 $prime$ 為空串列， $max\_p = 0$
2. 使用上述方法，找到 $n$ 的第一個質因數 $a$ ，並將 $n$ 分解為 $a * m$
3. 將 $n$ 設定為 $m$ ，如果 $a$ 不在串列 $prime$ 中，將 $a$ 附加在串列 $prime$ 中，且將 $max\_p$ 設為 $a$
4. 如果停止條件成立，停止，否則跳到步驟2執行

goto

## 步驟

1. 輸入 $n$ ，設定`prime`為空串列， $\text{max\_p} = 0$
2. `while n > max_p:`
  - A. 使用上述方法，找到 $n$ 的第一個質因數 $a$ ，並將 $n$ 分解為 $a * m$
  - B. 將 $n$ 設定為 $m$ ，如果 $a$ 不在串列`prime`中，將 $a$ 附加在串列`prime`中，且將 $\text{max\_p}$ 設為 $a$

輸入n，設定  
prime為空  
串 列 ，  
max\_p = 1

```
import random
S = list(range(1,100000))
n = random.choice(S)
prime = []
max_p = 1
while n > max_p:
    for a in range(2,n):
        if n % a == 0:
            m = n//a
            print(n, 'equals', a, '*', m)
            break
        else:
            print(n, 'is a prime number')
            a = n
            m = 1
    n = m
    if not a in prime:
        prime.append(a)
        max_p = a
print(prime)
```

找n的最  
小質因數

```

import random
S = list(range(1,100000))
n = random.choice(S)
prime = []
max_p = 1
while n > max_p:
    for a in range(2,n):
        if n % a == 0:
            m = n//a
            print(n, 'equals', a, '*', m)
            break
        else:
            print(n, 'is a prime number')
            a = n
            m = 1
            n = m
            if not a in prime:
                prime.append(a)
                max_p = a
print(prime)

```

找n的最小質因數，  
將n分解為  
 $a * m$

B. 將n設定為m，如果a不在串列prime中，將a附加在串列prime中，且將max\_p設為a

```
import random
import numpy as np
S = list(range(1,100000))
n = random.choice(S)
prime = []
max_p = 1
while n > max_p:
    for x in range(2, int(np.ceil(n / 2))):
        if n % x == 0:
            print('n = ', n, ' a = ', x)
            a = x
            m = n // a
            break
    else:
        print('n is a prime ', n)
        a = n
        m = n // a

    n = m
    if not a in prime:
        prime.append(a)
        max_p = a
print(prime)
```

# 兩個陣列相加

## 陣列

```
import numpy as np  
a = np.array([1,2])  
print(a)  
b = np.array([3,4])  
print(b)  
print(a+b)
```

```
[1 2]  
[3 4]  
[4 6]
```

## 串列

```
p=[1,2]  
q=[3,4]  
p+q
```

```
>>> p=[1,2]  
>>> q=[3,4]  
>>> p+q  
[1, 2, 3, 4]
```

**陣列size, max, min, mean**

```
a = np.array([1,2, 3 ,5, 7])  
print(a.size, a.max(),a.min(),a.mean())
```

```
>>> a = np.array([1,2, 3 ,5, 7])  
... print(a.size,a.max(),a.min(),a.mean())  
5 7 1 3.6
```

# 陣列元素加總

```
a = np.array([1,2, 3 ,5, 7])  
print(np.sum(a))
```

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# 陣列相乘

```
a = np.array([1,2, 3 ,5, 7])  
print(np.multiply(a,a))  
print(a*a)
```

```
>>> a = np.array([1,2, 3 ,5, 7])  
... print(np.multiply(a,a))  
... print(a*a)  
[ 1  4  9 25 49]  
[ 1  4  9 25 49]
```

# 二維陣列，矩陣

```
A = np.array([[1,2,3],[4,5,6],[7,8,9]])  
print(A)  
print(A.size)
```

```
[ [1 2 3]  
  [4 5 6]  
  [7 8 9]]
```

```
9
```

```
A = np.array([[1,2,3],[4,5,6],[7,8,9]])  
print(A)  
print(np.transpose(A))
```

```
[[1 2 3]  
 [4 5 6]  
 [7 8 9]]  
[[1 4 7]  
 [2 5 8]  
 [3 6 9]]
```