

1. Write a matlab function to implement the first type of row operation, $\text{row_op1}(A, i, s)$, where the operation multiplies the i th row of matrix A by a scalar s .
2. Apply row_op1 to calculate the result of multiplying the second row of A by 2

$$\begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 3 & 3 & -3 & 9 & 12 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 6 & 6 & -6 & 18 & 24 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}$$

3. Write a matlab function to implement the second type of row operation, $\text{row_op2}(A, i, j)$, where the operation swaps the i th row and the j th row of matrix A .
4. Apply row_op2 to swap the first and second rows of matrix A .

$$\begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 3 & 3 & -3 & 9 & 12 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}
 \longrightarrow
 \begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 3 & 3 & -3 & 9 & 12 \\
 0 & 0 & 2 & -2 & 2 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}$$

5. Write a matlab function to implement the type III row operation, $\text{row_op3}(A, i, j, s)$, where the operation returns a matrix that is a result of adding s times row j to row i .
6. Apply row_op3 to add 2 times row 3 to row 2 of matrix A .

$$\begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 3 & 3 & -3 & 9 & 12 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}
 \xrightarrow{R_2 + 2 * R_3}
 \begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 11 & 11 & -7 & 31 & 36 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}$$

7. Write a script to perform row operations that translate matrix A to its reduced echelon form.

$$\begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 0 & 0 & 2 & -2 & 2 \\
 3 & 3 & -3 & 9 & 12 \\
 4 & 4 & -2 & 11 & 12
 \end{array}
 \end{array}
 \xrightarrow{\text{Row operations}}
 \begin{array}{c}
 \mathbf{A} = \\
 \begin{array}{ccccc}
 1 & 1 & 0 & 0 & 17 \\
 0 & 0 & 1 & 0 & -5 \\
 0 & 0 & 0 & 1 & -6
 \end{array}
 \end{array}$$

8. Write a Matlab function to implement the algorithm my_rref for determining the reduced echelon form of a matrix.

function B=my_rref(A)

```
B=A;
[M N]=size(B);
pivot_col = 0;
```

```
for i = 1:M
    for j=pivot_col+1:N

        find the first non-zero element of col j from row i to row M
        if such element exist
            use it to create a leading 1 for row i
            eliminate other elements in column j
            pivot_col=j;
            break
        end
    end
end
```

Exercise 8
Write a Matlab function to implement my_rref

9. Apply the Matlab function my_rref to translate the following matrix to a reduced echelon form.

$$\mathbf{A} = \begin{bmatrix} 0 & 0 & 2 & -2 & 2 \\ 3 & 3 & -3 & 9 & 12 \\ 4 & 4 & -2 & 11 & 12 \end{bmatrix} \xrightarrow{\text{my_rref}} \mathbf{A} = \begin{bmatrix} 1 & 1 & 0 & 0 & 17 \\ 0 & 0 & 1 & 0 & -5 \\ 0 & 0 & 0 & 1 & -6 \end{bmatrix}$$

10. Apply the Matlab function my_rref to invert the following matrix.

$$A = \begin{bmatrix} 1 & -1 & -2 \\ 2 & -3 & -5 \\ -1 & 3 & 5 \end{bmatrix}$$